Conceptual Design of Single-Acting Oleo-Pneumatic Shock Absorber in Landing Gear with Combined Method

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Abstract
Landing gear is a structure that is mounted under the fuselage and helps the aircraft in takeoffs and landings. The most important duty of landing gear is the control of vibration exerted on the system through the shock absorber which is a common component to all the landing gear. Considering the importance of this issue, the necessity of investigating shock absorber with features such as high efficiency, reliability and maintenance, etc. is undeniable. In the present study In addition to choosing hydro pneumatic shock absorber its relationships arising from oil and gas liquids have been studied. This research was conducted with the aim of reducing the force variations and vibrations, with a focus on liquid gas. Thus, according to the gas laws, initially gas flow in the case of practical modes of isotherms during the taxi and poly trophic during landing has been studied. Considering that in the shock absorber only one mode can be used and Isotherms mode despite less vibration is not responsible for the landing phase and poly trophic mode exerts a lot of vibration on the fuselage, therefore a situation that can meet both needs in a way that have both phases of taxiing and landing and at the same time reducing vibrations to be followed is the combination mode that its relation has been extracted at the end. The results of the extracted relations using numerical methods compared with practical results shows that not only the force on the aircraft body but also the vibrations on it have been significantly reduced and improves system performance.

Keywords: landing gear, vibration, fluid, gas, shock absorber, hydro pneumatic shock absorber;

1- Introduction
In each plane shock absorber mechanism which applied during landing and take-off and guides the aircraft on the ground is particularly important. (Michalowski, 2007; Anon, 1994) shock absorber is one of the most important components of all landing gear as all existing aircraft doesn’t have a Tires, wheels, brakes and … but all of them have somehow shock absorber. The main duty and function of a shock absorber, as its name implies, is absorbing and damping kinetic energy of the impact to the extent that acceleration imposed on the fuselage reduced to the minimum tolerable (Currey, 1988). In general, there are two main types of shock absorber depending on the type of spring used in it. A kind of shock absorber, which is called mechanical shock absorber, composed from solid spring steel or rubber and other type is formed from a gas spring or oil or a mixture of them which the latter type is known respectively pneumatic, hydraulic
and hydro pneumatic shock absorber. According to research carried out it can be realized that hydro pneumatic shock absorber in terms of high efficiency and optimum weight (Currey, 1988; Bauer, 2011) features spring, damping characteristics, level control, design space and cost in comparison with the other shock absorbers listed have very tangible advantage. That is why in various industries wide acceptance of this type dampers are made. The study focused on the design of this type shock absorber.

2- Types of shock absorber

As mentioned in the introduction mechanical dampers are one of shock absorbers. This type of shock absorber have lost their capability in various applications due to the very high weight, low efficiency which is about 60% (Currey,1988), monotonic and fixed flexibility ratio in the move as well as unavailability of the control level (Currey,1988). Another type of the shock absorber is formed from a gas flow or oil or a mixture of them. The gas flow mode which is referred to pneumatic shock absorber has been used less in recent years because of heavy weight, low efficiency and reliability (Michalowski, 2007). And also the need to a relatively large design space compared to hydro-pneumatic system (Currey, 1988; Bauer, 2011). The oil mode which is the hydraulic shock absorber, despite the high efficiency of about 75 to 90%, which compete in this respect with hydro pneumatic shock absorber, but need to bear the high pressure fluid, weight increase and its performance has changed. As well as changes in the volume of fluid at low temperatures has affected the efficiency of the shock absorber. The mixture of oil and gas mode which is known as hydro-pneumatic shock absorber, created a revolution in landing gear growth in the United States in 1950 (Bauer,2011). These shock absorbers for having both fluid and gas flow can benefit from the advantages of both previous states. Such a way that by gas absorbs energy and by the oil damped it (Currey, 1988). Therefore, due to increase flexibility coefficient (Currey, 1988; Bauer, 2011) and the highest level of friction and damping (Currey, 1988), have the highest efficiency between 80 to 90% and also have the highest energy dissipation (Michalowski, 2007; Anon, 1994). Table 1 compares these shock absorbers so that the efficiency of hydropneumatic suspension system was clear.

Table 1: Comparison of shock absorbers (Bauer, 2011)

<table>
<thead>
<tr>
<th></th>
<th>Mechanical spring and damper</th>
<th>Pneumatic spring and damper</th>
<th>Hydro pneumatic system</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spring characteristics</td>
<td>0</td>
<td>++</td>
<td>++</td>
</tr>
<tr>
<td>Damping and friction characteristics</td>
<td>++</td>
<td>++</td>
<td>+</td>
</tr>
<tr>
<td>Control level</td>
<td>-</td>
<td>+</td>
<td>++</td>
</tr>
<tr>
<td>Cost</td>
<td>++</td>
<td>0</td>
<td>-</td>
</tr>
<tr>
<td>Design space requirement</td>
<td>0</td>
<td>-</td>
<td>+</td>
</tr>
<tr>
<td>Reliability + robustness</td>
<td>+</td>
<td>0</td>
<td>+</td>
</tr>
<tr>
<td>Service requirements</td>
<td>+</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

3- Single-chamber hydro-pneumatic shock absorber

According to figure 1, in these shock absorbers, shock absorber cylinder is two chambers. Upper and lower chambers are separated by orifice plate which orifice in which is embedded. When the force is
applied to shock absorber, fluid through the orifice move between the upper and lower chamber. By moving hydraulic fluid from the lower chamber to the upper, the gas pressured which increases its pressure and thus produces a force as gas spring force. When this gas which can be dry air or nitrogen compressed serves as a spring.

Figure 1: sketch of a hydropneumatic shock absorber

Orifice along with metering pin that provides changes in the size of the orifice, control the damping characteristics of the shock absorber when the metering pin through the orifice moves. Therefore, it is essential two independent conditions to be formulated.

4- Formulation of the forces

According to the expressed contents shock absorber force, \(F_s\), can be calculated by the following equation.

\[
F_s = (P_u - P_l)A_L + P_s(A_u - A_L) = F_p + F_g \tag{1}
\]

Where \(P_l\) and \(A_L\) are respectively pressure and the upper lower area, \(P_u\) and \(A_u\) pressure and the upper chamber area and \(P_g\) the Reservoir pressure which is \(P_u = P_g\).

In Equation (1) the shock absorber force is considered as a combination of the force caused by the pressure drop in the orifice and gas spring force. \(F_p\) Force can be a linear relationship between the force and pressure and a nonlinear relationship between Force and speed which by considering the law of conservation of mass for an incompressible fluid is as follows (Currey, 1988; Batterbee et al, 2007).

\[
F_p = (P_u - P_l)A_L = \Delta P A_L \tag{2}
\]

Given that pressure drop in the orifice, \(\Delta P\), depends on the factors such as flow rate, orifice geometry, orifice size and density of the hydraulic fluid therefore, at first it is necessary to find a logical relationship between the pressure difference and the mentioned factors that it would be achieved through the following equation:
\[ \Delta P = Q^2 K_B \]  

(3)

Where \( Q \) is the volumetric flow rate which directly related to the flow rate, \( K_B \), a constant value which depends on the geometry, orifice size and density of the hydraulic fluid and through the following relations are defined:

\[ Q = A_2 \dot{x}_1 \]  

(4)

\[ K_B = \frac{8 \rho}{\alpha_D^2 \pi^2 d_{orifice}^4} \]  

(5)

Where \( \dot{x}_2 \) is flow rate, \( \rho \) fluid density, \( d_{orifice} \) the diameter of the orifice and \( \alpha_D \) flow coefficient which depends on the geometry of the edge. Note that this flow rate is the relative speed of the shock absorber. Thus, by replacing equations (4) and (5) at equation (3) and then equation (2) we have: (Bauer,2011)

\[ \Delta P = (A_2 \dot{x}_2)^2 \frac{8 \rho}{\alpha_D^2 \pi^2 d_{orifice}^4} \]  

(6)

\[ F_g = A_2^3 \dot{x}_2^2 \frac{8 \rho}{\alpha_D^2 \pi^2 d_{orifice}^4} \]  

(7)

“Fig. 2” shows that Minimum flow rate \( \alpha_D \) can be 1 and here because of drawing charts and conclusions for selected shock absorber, 1 is considered.

Gas spring force is also \( F_g \) which is as follows:

\[ F_g = F_g (A_u - A_2) \]  

(8)

To obtain the relationship between gas pressures the polytropic gas law for a closed system can be used (Currey, 1988).

\[ P_{gs} V_{gs}^n = P_{gs} V_{gs}^{n} = C \]  

(9)

Where \( P_{gs} \) And \( V_{gs} \) are respectively pressure and gas volume in each stroke, \( P_{gs} \) and \( V_{gs} \) are pressure and gas volume at full extension, \( C \) is a constant and \( n \) is an exponent which depends on the rate of compression.

Since the volume, \( V_{gs} \), can be written as a function of stroke, \( S_x \), So:

\[ V_{gs} = V_{gs} - A_u S_x \]  

(10)

So in each stroke, \( x \), we have:

\[ P_{gs} = P_{gs} \left( \frac{V_{gs}}{V_{gs}} \right)^n \]  

(11)

Where: \( \cdot \leq S_x \leq S_{tot} \)

By replacing \( P_{gs} \) into the equation (3) we have:

\[ F_{gs} = (A_u - A_2) P_{gs} \left( \frac{V_{gs}}{V_{gs} - A_u S_x} \right)^n \]  

(12)
Where: \( 0 \leq S_x \leq S_{\text{tot}} \)

For the normal ground handling, when the compression is low, the process is isothermal and \( n = 1 \) and for dynamic (fast) compression cases such as landing impact, where the compression is high, polytropic process is applied in which \( n > 1 \). In this process, \( n = 1.1 \) or \( n = 1.35 \) can be considered. The former is used when the gas and oil are separated and the latter when they are mixed during compression (Michalowski, 2007; Currey, 1988).

So it can be concluded:

\[
F_{g_{\text{poly}}} = F_{g_{x}} \quad n > 1
\]

\[
F_{g_{\text{iso}}} = F_{g_{x}} \quad n = 1
\]

Since there is only one shock absorber in any aircraft for the normal ground handling and dynamic modes such as landing phase, so such a shock absorber should be designed to meet both needs. For this purpose it would be more appropriate to design based on the polytropic to include the normal mode too.

It is important to note to maximum pressure (pressure at full compression) in polytropic mode. If this pressure is smaller than the allowable pressure at this point, the polytropic method will be the basis of design.

But if in computing, a greater allowable pressure at this point is achieved, the best method is combined method that's mean using the polytropic and Isotherm at the same time (Currey, 1988).

When using this method (combined method), it is better to use isotherm method from the fully extended point to static point and use polytropic method from the static point to fully compressed point. Therefore, we have the following relationship:

Fully extended to static:

\[
P_{g_{x}} = \frac{P_{g_{x}}V_{g_{x}}}{V_{g_{x}}^{n}}
\]

\[
P_{g_{x}} = \frac{P_{g_{x}}V_{g_{x}}}{V_{g_{x}} - A_{g_{x}}S_{x}}
\]

Where: \( 0 \leq S_x \leq S_{\text{static}} \)

\[
F_{g_{x}} = (A_{u} - A_{L})F_{g_{x}}
\]

\[
F_{g_{x}} = (A_{u} - A_{L}) \frac{P_{g_{x}}V_{g_{x}}}{V_{g_{x}} - A_{g_{x}}S_{x}}
\]

Where: \( 0 \leq S_x \leq S_{\text{static}} \)

And static to fully compress:

\[
P_{g_{x}} = P_{\text{static}} \left( \frac{V_{\text{static}}}{V_{g_{x}}} \right)^{n}
\]

\[
P_{g_{x}} = P_{\text{static}} \left( \frac{V_{\text{static}}}{V_{g_{x}} - A_{g_{x}}S_{x}} \right)^{n}
\]

Where: \( S_{\text{static}} \leq S_{x} \leq S_{\text{compress}} \)

So it can be concluded:

\[
F_{g_{\text{comb}}} = F_{g_{x}} + F_{g_{x}}
\]

In order to better understand this issue and how to use the combination method, a sample shock absorber is examined. The sample shock absorber has a static pressure of 1500 psi and a course in 20.

In order to achieve a favorable shock absorber, it is first necessary to determine which compression ratio is used.

The compression ratio is a pressure ratio at one point (for example, in a fully dense
mode) divided by pressure at another point (for example, in a completely open state). Usually, two compression ratios are considered, both of which are as follows: The first ratio is the fully open state to the static state, and the other is the static state to a fully dense state. For large aircraft, the following ratios can be used [3]:

\[
\text{Static mode to open state } = r_{se} = \frac{4}{1}
\]

\[
\text{Density mode to static} = r_{se} = \frac{3}{1}
\]

First, calculations are made for the isotherm state:

**Isotherm calculations:**

\[ S = \text{total stroke} = 20 \text{ in} \]

\[ F_s = \text{static force} = 50000 \text{ lb} \]

\[ p_s = \text{static pressure} = 1500 \text{ psi} \]

Then:

\[ P_1 = P_s = 1/r_{se} \times P_2 = 1/4 \times 1500 = 375 \quad \text{in (18)} \]

\[ P_2 = P_f = 1500 \text{ psi} \]

\[ A_u = \frac{F_s}{P_s} = \frac{50000}{1500} = 33.33 \quad \text{in (19)} \]

\[ A_u = \frac{F_s}{P_f} = \frac{50000}{1500} = 33.33 \quad \text{in (20)} \]

Displacement volume \( D = \text{piston area x stroke} = 33.33 \times 20 = 666.7 \text{ in} \)

\[ V_1 - V_3 = D, \quad V_3 = V_1 - D \]

\[ P_1 V_1 = P_3 V_3 = \text{cons} \quad \text{(22)} \]

\[ V_1 = \frac{P_1 (V_1 - D)}{P_3} = \frac{4500(V_1 - 666.7)}{375} = 727.3 \]

\[ V_3 = V_1 - D = 727.3 - 666.7 = 60.6 \quad \text{(23)} \]

\[ V_2 = \frac{P_2 V_3}{P_2} = \frac{1500 \times 727.3}{1500} = 181.4 \quad \text{(24)} \]

Briefly:

\[ P_1 = 375, \quad V_1 = 727.3, \quad F_1 = 12500 \]

\[ P_2 = 1500, \quad V_2 = 181.4, \quad F_2 = 50000 \]

\[ P_3 = 4500, \quad V_3 = 60.6, \quad F_3 = 150000 \]

Now due to high values and with the help of the equation \( P_x = \frac{P_1 V_1}{V_1 - A_u S_x} \), Pressure at any other point followed by equation \( P_x = \frac{P_1 V_1}{V_1 - A_u S_x} \), the volume proportional to the desired pressure is obtained.

**Polytropic calculations**

In order to compare this state with isotherm state, in addition to the same consideration of volumes, the initial pressure is also the same; therefore:

\[ V_1 = 727.3 \]

\[ V_3 = 60.6 \]

\[ P_1 = 375 \]

So having the high values according to the equation \( P_x = \frac{P_1 (V_1)}{V_1 - A_u S_x}^{1.38} \), It is easy to
obtain pressure at any desired position for the polytropic state.

For example, in order to get $P_3$, taking into account the course $S_x = 20$, the pressure value is in the compressed state of

$$P_3 = P_1 \left( \frac{V_1}{V_1 - A_S x} \right)^{1.35} = 375 \left( \frac{727.3}{227.3 - (25.13 \times 26)} \right)^{1.35} = 10740.1$$

Briefly:

$P_1 = 375$, $V_1 = 727.3$, $F_1 = 12500$

$P_2 = 1500$, $V_2 = 260.4$, $F_2 = 50000$

$P_3 = 10740.1$, $V_1 = 60.6$, $F_3 = 357970$

Now, the pressure in the point of the compressed state in the polytropic state is the pressure in the course 20, that’s $P_5$, is checked in order to be smaller than the limit.

Given the selective shock absorber and the course and static pressure, it can be said that $P_5$ should be less than 6000 psi to prevent leakage. But somewhat higher than is acceptable. ($6000 < 1/10740$)

The combined calculation (isotherm and polytropic state)

As it was observed in the isotherm state, the pressure obtained was not responsive to the polytropic state; in the polytropic state, the pressure at the compressed point was greater than the permissible pressure to prevent leakage; For this reason, in order to obtain optimal mode, a combination mode is used which is further discussed.

Regarding the equation

$$P_x = \frac{P_1 V_1}{V_1 - A_u S_x}$$

having $P_2$ and $V_2$ Similar to what was said in the isotherm calculations, and taking $S_x$ from zero to the course in a static state, the isotherm pressures in the range of 0 to the static course are obtained for this condition. But for its polytropic mode, according to the equation $P_x = P_2 \left( \frac{V_2}{V_1 - A_s S_x} \right)^n$

having $P_2$ and $V_2$ which is obtained by putting $S_x = S_{static}$ in the preceding relationship, and also having $V_1$ by taking $S_x$ from a static point to a very compressed point, From a static point to a perfectly compressed point, the polytropic pressures are obtained in this combined state.

Briefly, for the isotherm section:

$P_1 = 375$, $V_1 = 727.3$, $F_1 = 12500$

$P_2 = 1500$, $V_2 = 181.4$, $F_2 = 50000$

So the course of the open state becomes static by the following equation:

$$S_2 = (V_1 - V_2) / A_u = 16.8$$  \hspace{1cm} (26)$$

And in brief, for the polytropic section:

$P_2 = 1500$, $V_2 = 181.4$, $F_2 = 50000$

$P_3 = 5645.3$, $V_3 = 60.6$, $F_3 = 188160$

As can be seen, $P_3 = 5645.3$, unlike the polytropic state, is less than 6000. The results of the sample shock absorber are shown in Table 1.
Table 1: the Calculation of the density of combined mode

<table>
<thead>
<tr>
<th>Stroke (in)</th>
<th>V (in^3)</th>
<th>Pvap (psi)</th>
<th>Pcond (psi)</th>
<th>Pevap (psi)</th>
<th>Fcond (lb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>727.3</td>
<td>375</td>
<td>375</td>
<td>375</td>
<td>12500</td>
</tr>
<tr>
<td>4.0</td>
<td>593.9</td>
<td>459.2</td>
<td>493</td>
<td>459.2</td>
<td>15306.7</td>
</tr>
<tr>
<td>8.0</td>
<td>460.6</td>
<td>592.1</td>
<td>694.8</td>
<td>592.1</td>
<td>19736.7</td>
</tr>
<tr>
<td>12.0</td>
<td>327.3</td>
<td>833.3</td>
<td>1102</td>
<td>833.3</td>
<td>27776.7</td>
</tr>
<tr>
<td>16.0</td>
<td>193.9</td>
<td>1406.5</td>
<td>2234.2</td>
<td>1406.5</td>
<td>46883.6</td>
</tr>
<tr>
<td>20.0</td>
<td>60.6</td>
<td>4500.6</td>
<td>10740.1</td>
<td>5645.3</td>
<td>188160</td>
</tr>
</tbody>
</table>

5. Equations of motion

In order to investigate the vibrations on the fuselage in three modes of isotherms, polytropic and combinations, the equations of motion of the landing gear with two degree of freedom is obtained in which the whole aircraft body is assumed as a rigid body mass (the upper mass) and tire is modeled by a rigid body mass (The lower mass), spring and damper.

\[
\frac{W_u}{g} \ddot{x}_u + F_s - W_u + F_t - W_L = 0. \tag{28}
\]

Where \(W_u\) is the airframe weight and \(W_L\) is the wheel tire weight. It is noted that \(x_u\) and \(x_L\) are measured from the positions of \(W_u\) and \(W_L\) at the instant \(t = \cdot\) when the tire first contacts the ground. \(\ddot{x}_u\) and \(\ddot{x}_L\) are the upper and lower mass accelerations respectively and \(g\) is the gravitational acceleration.

\(F_t\) is the tire force which represented here as:

\[
F_t = \begin{cases} 
  k_t x_L + c_t \dot{x}_L, & x_L > \cdot \\
  0, & x_L \leq \cdot
\end{cases} \tag{29}
\]

Where \(k_t\) is the tire stiffness and \(c_t\) is damping coefficient of the tire. \(F_L\) is the lift force exerted from the air on the aircraft body and has upward direction. During the landing, the lift force varies and can be expressed as a function of time by an equation given by Choi and Wereley. (Choi, 2003)

\[
F_L = [1.2 - 0.9 \tanh(3t)](W_u + W_L) \tag{30}
\]

Where \(t \geq \cdot\) is the time in seconds.
6. Conclusions

In this study, the hydromechanical shock absorber was selected as the most favorable shock absorber in comparison with mechanical, hydraulic and non-mechanical shock absorber. After expressing the fluid relation in this system, the gas relations were investigated in isotherm and polytropic modes. Considering the permissible shear stress of the cylinder, it was determined that if the polytropic mode pressure is exceeded, then the combination mode, which is an optimal mode for reducing the forces and vibrations entering the system, is selected. According to the values considered for selected shock absorber in Table 2 and force-stroke curve plotted in isotherm, polytropic and combined modes in Figure 4, it is concluded that polytropic mode due to its larger force from the permissible force shown in Table 3 cannot be used in such a landing gear therefore the combined mode is substituted. “Fig. 5” illustrates that when using combined mode, not only the pressure required at the time of taxing and landing is provided, but also the vibration and dynamic loads attenuate and consequently decrease the acceleration transmitted to the fuselage during the touch-down impact in landing. In other words, pressure is the pressure required in landing phase while the vibrations are as taxi phase which its results can be seen Table 4. The interesting point in the figure (5) is that as time passes and vibration drops, Domain is not zero. The reason is that the static state of the course (static mode of the aircraft), which is visible in the figure (5-a) is other than point zero; Therefore, due to the dropping of the body of the aircraft at a static point, the damping domain will be at the static point.

Now that the applicability of the combined method has become clearer than the two methods mentioned, it is important that the results are checked with various parameters such as the diameter of the orifice, speed ... which will be addressed in the next research.

Table 2: values of selected shock absorber

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Upper chamber</td>
<td>$A_u \cdot m^2$</td>
</tr>
<tr>
<td>Lower chamber</td>
<td>$A_L \cdot m^2$</td>
</tr>
<tr>
<td>Fully extended gas pressure</td>
<td>$P_{gs} \cdot kpa$</td>
</tr>
<tr>
<td>Fully extended gas volume</td>
<td>$V_{ge} \cdot m^3$</td>
</tr>
<tr>
<td>Orifice diameter</td>
<td>$d_{orifice} \cdot m$</td>
</tr>
<tr>
<td>Fluid density</td>
<td>$\rho \cdot kg/m^3$</td>
</tr>
<tr>
<td>Weight of the airframe</td>
<td>$M_a \cdot kg$</td>
</tr>
<tr>
<td>Weight of the tire</td>
<td>$M_t \cdot kg$</td>
</tr>
<tr>
<td>Tire stiffness</td>
<td>$K_t \cdot KN/m$</td>
</tr>
<tr>
<td>Tire damping coefficient</td>
<td>$C_t \cdot N.s/m$</td>
</tr>
</tbody>
</table>

Table 3: Optimal results of shock absorber force at fully compressed point

<table>
<thead>
<tr>
<th>Mode</th>
<th>Force at fully compressed point of shock absorber</th>
<th>Allowable pressure force</th>
<th>Improvement of combined to polytropic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Polytropic</td>
<td>84200</td>
<td>60000</td>
<td>%40.26</td>
</tr>
<tr>
<td>Combined</td>
<td>50300</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 4: Optimal results of fuselage displacement

<table>
<thead>
<tr>
<th>Mode</th>
<th>Isotherm</th>
<th>Polytropic</th>
<th>Combined</th>
<th>Improvement of combined to polytropic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Upper mass or fuselage displacement (m)</td>
<td>-0.4783</td>
<td>-0.5832</td>
<td>-0.4794</td>
<td>% 17.8</td>
</tr>
</tbody>
</table>

1 It should be noted that the author has used MR (Magnetic Rheological) fluid containing magnetic particles.
References


